

# ATM 500: Atmospheric Dynamics

## Homework 6

Due Monday October 25 2021

1. Suppose that in a hydrostatic atmosphere in the southern hemisphere, temperatures increase northward on every pressure level between the surface and the tropopause. Also suppose that the pressure gradient force is zero on the 500 hPa surface (about halfway between the surface and tropopause). Make a sketch that shows how the slope of pressure surfaces and the geostrophic winds must vary with height. Make sure to explain your reasoning. What is the direction of the geostrophic wind near the surface? What about near the tropopause? (Use the meteorological convention: “westerly” = from the west, “northerly” = from the north, etc.)
2. In meteorological terminology, “veering” winds turn clockwise with increasing height, while “backing” winds turn anti-clockwise with increasing height. Show that for an atmosphere in thermal wind balance, veering winds must be associated with *warm air advection*. Also show that backing winds must be associated with cold air advection.
3. *Based on Question 3.3 from Vallis*

Consider a rapidly rotating (i.e., in near geostrophic balance) Boussinesq fluid on the  $f$ -plane.

- a. Show that the pressure divided by the density scales as  $\phi \sim fUL$ .
  - b. Show that the horizontal divergence of the geostrophic wind vanishes. Thus, argue that the scaling  $W \sim UH/L$  is an *overestimate* for the magnitude of the vertical velocity. Obtain a scaling estimate for the magnitude of vertical velocity in rapidly rotating flow.
  - c. Using these results, or otherwise, discuss whether hydrostatic balance is more or less likely to hold in a rotating flow than in non-rotating flow.
4. *Based on Question 3.7 from Vallis*

Estimate the magnitude and direction of the zonal wind 5 km above the surface in the mid-latitude atmosphere in summer and winter using (approximate) values for the meridional temperature gradient in the atmosphere. Compare your estimated value to a typical climatological zonal wind at this same location. Make sure to cite your data sources and state any assumptions you make.